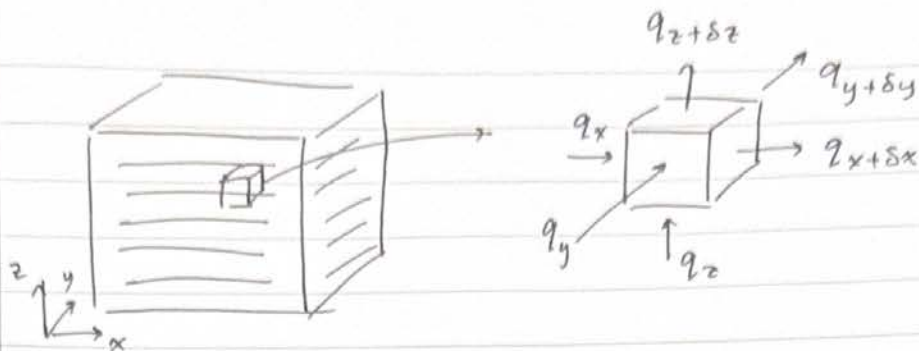


a)



$$\rho \delta V c \frac{\partial T}{\partial t} = (q_x - q_{x+\delta x}) \delta y \delta z + (q_y - q_{y+\delta y}) \delta x \delta z + (q_z - q_{z+\delta z}) \delta x \delta y$$

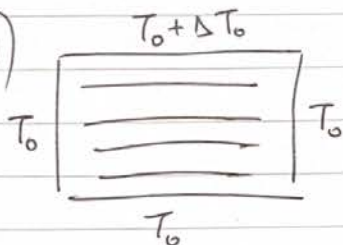
$$\Rightarrow \rho \delta x \delta y \delta z c \frac{\partial T}{\partial t} = -\frac{\partial q_x}{\partial x} \delta x \delta y \delta z - \frac{\partial q_y}{\partial y} \delta x \delta y \delta z - \frac{\partial q_z}{\partial z} \delta x \delta y \delta z$$

$$\Rightarrow \rho c \frac{\partial T}{\partial t} = \lambda_{||} \frac{\partial^2 T}{\partial x^2} + \lambda_{||} \frac{\partial^2 T}{\partial y^2} + \lambda_{\perp} \frac{\partial^2 T}{\partial z^2}$$

$$\Rightarrow \boxed{\frac{\partial T}{\partial t} = \alpha_{||} \frac{\partial^2 T}{\partial x^2} + \alpha_{||} \frac{\partial^2 T}{\partial y^2} + \alpha_{\perp} \frac{\partial^2 T}{\partial z^2}}$$

$$\alpha_x = \frac{\lambda_{||}}{\rho c} ; \alpha_y = \frac{\lambda_{||}}{\rho c} ; \alpha_z = \frac{\lambda_{\perp}}{\rho c}$$

b) i)



No variation in y or t:

The governing equation is

$$\alpha_{||} \frac{\partial^2 T}{\partial x^2} + \alpha_{\perp} \frac{\partial^2 T}{\partial z^2} = 0$$

Introduce a reduced temperature $\Theta = \frac{T - T_0}{\Delta T}$

Boundary conditions: $\Theta(x=0, z) = 0$
 $\Theta(x=W, z) = 0$
 $\Theta(x, z=0) = 0$
 $\Theta(x, z=H) = 1$

} homogeneous

Governing equation $\alpha_{||} \frac{\partial^2 \Theta}{\partial x^2} + \alpha_{\perp} \frac{\partial^2 \Theta}{\partial z^2} = 0$

Separation of variables: $\Theta(x, z) = X(x) Z(z)$

$$\frac{\partial^2 \Theta}{\partial x^2} = X''Z ; \quad \frac{\partial^2 \Theta}{\partial z^2} = XZ''$$

$$\text{hence } \alpha_{||} X''Z + \alpha_{\perp} XZ'' = 0$$

$$\Rightarrow \frac{X''}{X} = - \frac{\alpha_{\perp}}{\alpha_{||}} \frac{Z''}{Z} = -\beta^2$$

↪ negative, because we expect sinusoidal variation in x , given the boundary conditions.

$$X'' + \beta^2 X = 0$$

$$\Rightarrow X = \sum_n a_n \sin \beta_n x + a'_n \cos \beta_n x$$

$$\text{at } x=0, X=0 : a'_n = 0$$

$$\text{at } x=W, X=0 : \sin \beta_n W = 0 \Rightarrow \beta_n = \frac{n\pi}{W}, \quad n \in \mathbb{N}$$

$$Z'' - \frac{\alpha_{\perp}}{\alpha_{||}} \beta^2 Z = 0 \quad \text{let } \gamma^2 = \frac{\alpha_{\perp}}{\alpha_{||}} \beta^2$$

$$\Rightarrow Z = \sum_n c_n \sinh \gamma_n z + c'_n \cosh \gamma_n z$$

$$\text{at } z=0, Z=0 : c'_n = 0$$

Combining the constants a_n & c_n :

$$\boxed{\Theta = \sum_n b_n \sin\left(\frac{n\pi x}{W}\right) \sinh\left(\sqrt{\frac{\alpha_{\perp}}{\alpha_{||}}} \frac{n\pi z}{W}\right), \quad n \in \mathbb{N}}$$

ii) at $z=H$, $\Theta=1$ for all x :

$$1 = \sum_n b_n \sin \frac{n\pi x}{W} \sinh \sqrt{\frac{\alpha_{\perp}}{\alpha_{||}}} \frac{n\pi H}{W}$$

To find b_n , we multiply both sides by $\sin \frac{n\pi x}{W}$, $n \in \mathbb{N}$ and integrate from 0 to W :

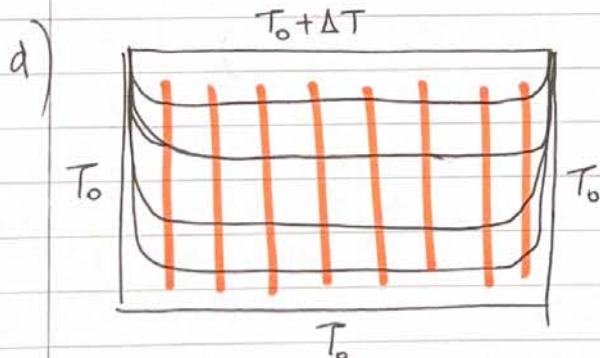
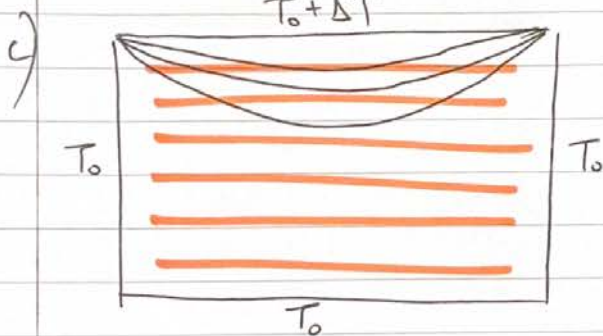
$$\int_0^W 1 \cdot \sin \frac{n\pi x}{W} dx = \int_0^W \sum_n b_n \sin \frac{n\pi x}{W} \sin \frac{n\pi x}{W} \sinh \sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi H}{W} dx$$

$$\Rightarrow -\frac{W}{n\pi} \left[\cos \frac{n\pi x}{W} \right]_0^W = \sum_n b_n \sinh \sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi H}{W} \underbrace{\int_0^W \sin \frac{n\pi x}{W} \sin \frac{n\pi x}{W} dx}_{\begin{aligned} &= 0 \text{ if } m \neq n \\ &= \frac{W}{2} \text{ if } m = n \end{aligned}}$$

$$\frac{W}{n\pi} (1 - \cos n\pi) = \frac{W}{2} b_n \sinh \sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi H}{W}$$

$$\Rightarrow b_m = \frac{2 [1 - (-1)^m]}{n\pi \sinh \sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi H}{W}}$$

$$\therefore \Theta(x, z) = \frac{T(x, z) - T_0}{\Delta T} = \sum_n \frac{2 [1 - (-1)^n]}{n\pi \sinh \left(\sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi H}{W} \right)} \sin \left(\frac{n\pi x}{W} \right) \sinh \left(\sqrt{\frac{\alpha_{\perp}}{\alpha_{\parallel}}} \frac{n\pi z}{W} \right)$$



Facile conduction in the $-z$ direction. Vertically stacked graphene sheets (above) act as poor conductors, while horizontally stacked sheets (left) conduct heat in the z -direction well.

$$\frac{\alpha_{\parallel}}{\alpha_{\perp}} = \frac{\lambda_{\parallel}}{\lambda_{\perp}} = \frac{2000}{5} = \underline{\underline{400}}$$

Q2 (a) N.S equation. Fully developed flow, steady state

$$\mu \frac{\partial^2 u_x}{\partial y^2} = \frac{dp}{dx}$$

τ constant

u - velocity along channel

BC 1 $\left. \frac{\partial u_x}{\partial y} \right|_{y=0} = 0$

BC 2 $u_x(y = \pm H) = 0$

$$u_x = \frac{dp}{dx} \frac{1}{2\mu} y^2 + C_1 y + C_2$$

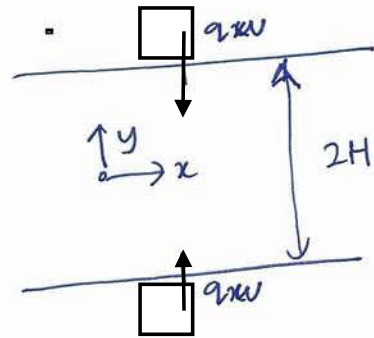
Using BC #1 $C_1 = 0$

using BC #2

$$0 = \frac{dp}{dx} \frac{1}{2\mu} H^2 + C_2$$

$$C_2 = -\frac{dp}{dx} \frac{1}{2\mu} H^2$$

$$u_x = -\frac{1}{2\mu} \frac{dp}{dx} (H^2 - y^2)$$



(b) $U_b = \frac{1}{2H} \int_{-H}^H u_x(y) dy$

$$= -\frac{1}{2H} \frac{dp}{dx} \frac{1}{2\mu} \int_{-H}^H (H^2 - y^2) dy$$

$$= -\frac{1}{2H} \frac{dp}{dx} \frac{1}{2\mu} \frac{4H^3}{3}$$

$$= -\frac{H^2}{3\mu} \frac{dp}{dx}$$

$$(c) \rho C_p \left(\cancel{\frac{\partial T}{\partial t}} + U_x \frac{\partial T}{\partial x} \right) = \alpha \frac{\partial^2 T}{\partial y^2}$$

steady state

$$U_x \frac{\partial T}{\partial x} = \alpha \frac{\partial^2 T}{\partial y^2}$$

$$\begin{aligned} U_x &= -\frac{1}{2\mu} \frac{dp}{dx} (H^2 - y^2) \\ &= -\frac{H^2}{2\mu} \frac{dp}{dx} \left(1 - \left(\frac{y}{H}\right)^2\right) \\ &= \frac{3}{2} U_b \left(1 - \left(\frac{y}{H}\right)^2\right) \end{aligned}$$

$$\frac{3}{2} U_b \left(1 - \left(\frac{y}{H}\right)^2\right) \frac{\partial T}{\partial x} = \alpha \frac{\partial^2 T}{\partial y^2}$$

$$(d) \quad G = \frac{dT}{dx} = \text{constant}$$

$$\frac{3}{2} U_b G \left(1 - \left(\frac{y}{H}\right)^2\right) = \alpha \frac{\partial^2 T}{\partial y^2}$$

$$\alpha \frac{\partial T}{\partial y} = \frac{3}{2} U_b G \left(y - \frac{y^3}{3H^2}\right) + C_1$$

BC1 Symmetric $\frac{\partial T}{\partial y} \Big|_{y=0} = 0$

$$\therefore C_1 = 0$$

$$\alpha T = \frac{3}{2} U_b G \left(\frac{y^2}{2} - \frac{y^4}{12H^2}\right) + C_2$$

BC2 $y=0 \quad T=T_0$

$$T = \frac{3}{2} \frac{U_b G}{\lambda} \left(\frac{y^2}{2} - \frac{y^4}{12H^2} \right) + T_0$$

Let's express the T to include q_w

$$-\lambda \frac{\partial T}{\partial y} \Big|_{y=H} = \dot{q}_w$$

$$-\lambda \frac{\rho c_p}{\lambda} \frac{3}{2} U_b G \left(H - \frac{H^3}{3H^2} \right) = \dot{q}_w$$

$$\dot{q}_w = -U_b G \rho c_p H$$

$$U_b G = -\frac{\dot{q}_w}{\rho c_p H}$$

$$\therefore T = -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(\frac{y^2}{2} - \frac{y^4}{12H^2} \right) + T_0$$

$$T(y=H) = -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(\frac{H^2}{2} - \frac{H^2}{12} \right) + T_0$$

$$= -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(H^2 \frac{5}{12} \right) + T_0$$

$$= -\frac{\dot{q}_w}{\lambda} \frac{5}{8} H + T_0$$

Given that $T_b = T_0 - \frac{\dot{q}_w H}{\lambda} \frac{39}{280}$

Heat transfer coefficient

$$h = \frac{\dot{q}_w}{|T_{\text{wall}} - T_{\text{b}}|}$$

$$h = \frac{\dot{q}_w}{|T(y=H) - T_{\text{b}}|}$$

$$h = \frac{\dot{q}_w}{0.486 \dot{q}_w H / \lambda} = \frac{\lambda}{0.486 H}$$

$$Nu = \frac{hD}{\lambda} = \frac{h(2H)}{\lambda}$$

$$= \frac{2}{0.486}$$

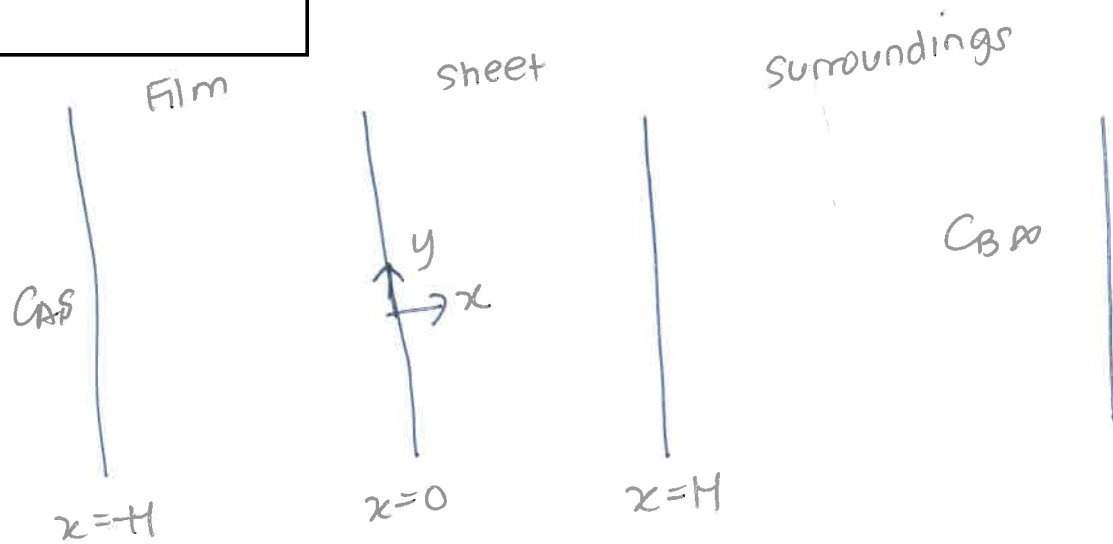
$$= 4.16$$

(f) Higher Nu number near the entrance.

Only a thin layer of fluid near the wall is heated

$$(T_{\text{wall}} - T_{\text{b}}) \sim \text{small}, \text{ so } Nu \uparrow$$

Q3



(a) Species A in Film only

$$D \frac{\partial^2 C_A}{\partial x^2} = 0$$

Species B in sheet only

$$D_B \frac{\partial^2 C_B}{\partial x^2} = 0$$

1-D problem

Boundary conditions

$$(1) C_A(x = -H) = C_{AS}$$

(2) At the film and sheet interface $x=0$

$$+D_A \frac{\partial C_A}{\partial x} \Big|_{x=0} = -k C_A(x=0)$$

$$(3) -D_B \frac{\partial C_B}{\partial x} \Big|_{x=0} = k C_A(x=0)$$

(4) Sheet to surrounding for B

$$-D_B \frac{\partial C_B}{\partial x} \Big|_{x=H} = h_m (C_B(x=H) - C_{B\infty})$$

Step 1 Solve $C_A(x)$

$$C_A(x) = C_1 x + C_2 \quad \left. \begin{matrix} C_1 \\ C_2 \end{matrix} \right\} \text{constants}$$

BC1 $C_A(x=-H) = C_{AS}$

$$C_{AS} = -H C_1 + C_2$$

BC2 $-D_A \frac{\partial C_A}{\partial x} \Big|_{x=0} = k C_A(x=0)$

$$-D_A C_1 = +k C_2$$

$$C_1 = -\frac{k}{D_A} C_2$$

$$C_{AS} = \frac{Hk}{D_A} C_2 + C_2$$

$$C_2 = \frac{C_{AS}}{1 + \frac{Hk}{D_A}}$$

$$\therefore C_1 = -\frac{k C_{AS}}{D_A + Hk}$$

$$C_A = \frac{C_{AS}(D_A - kx)}{D_A + Hk}$$

//

Solve for $C_B(x)$

$$C_B(x) = C_3 x + C_4 \quad \left. \begin{matrix} C_3 \\ C_4 \end{matrix} \right\} \text{constants}$$

BC $-D_B \frac{\partial C_B}{\partial x} \Big|_{x=H} = h_m (C_B(x=H) - C_{B\infty})$

$$-D_B C_3 = h_m (C_3 H + C_4 - C_{B\infty})$$

$$C_4 = C_{B\infty} - C_3 \left(\frac{D_B}{h_m} + H \right)$$

Next BC For B

$$-D_B \frac{\partial C_B}{\partial x} \Big|_{x=0} = h C_A(x=0)$$

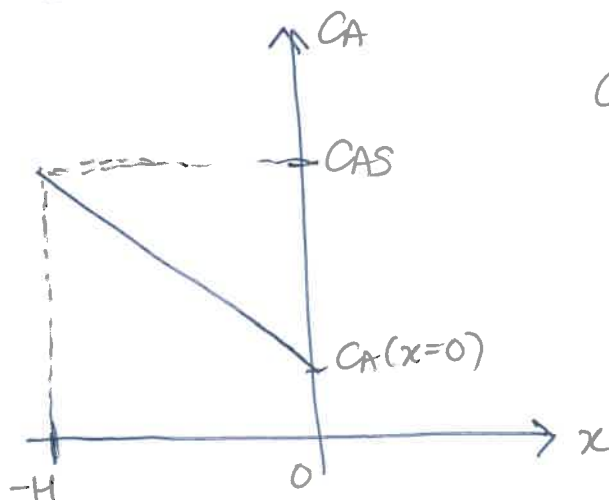
$$-D_B C_3 = k \frac{C_{AS} D_A}{D_A + Hk}$$

$$C_3 = -\frac{k}{D_B} \frac{C_{AS} D_A}{D_A + Hk}$$

$$\therefore C_4 = C_{B\infty} + \frac{C_{AS} D_A}{D_A + Hk} \left(\frac{k}{D_B} \right) \left(\frac{D_B}{h_m} + H \right)$$

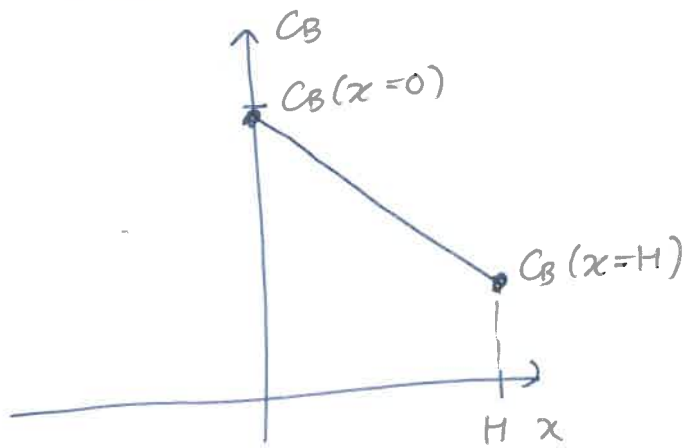
$$C_B(x) = -\frac{k}{D_B} \frac{C_{AS} D_A}{D_A + Hk} x + C_{B\infty} + \frac{C_{AS} D_A}{D_A + Hk} \left(\frac{k}{D_B} \right) \left(\frac{D_B}{h_m} + H \right)$$

Sketch



$$C_A(x=0) = \frac{C_{AS} D_A}{D_A + Hk}$$

Sketch C_B



diff by this term.

$$C_B(x=0) = C_{B\infty} + \frac{C_{A0} D_A}{D_A + Hk} \left(\frac{k}{D_B} \right) \left(\frac{D_B}{h_m} + H \right)$$

$$C_B(x=H) = C_{B\infty} + \frac{C_{A0} D_A}{D_A + Hk} \left(\frac{k}{D_B} \right) \left(\frac{D_B}{h_m} \right)$$

(c) $J_A = -D_A \frac{\partial C_A}{\partial x}$

$$= \frac{C_{A0} k D_A}{D_A + Hk} = \frac{C_{A0}}{\frac{1}{k} + \frac{H}{D_A}}$$

(d) we want the flux from the interface to the surrounding.

$$J_B = \frac{C_B(x=0) - C_{B\infty}}{\frac{H}{D_B} + \frac{1}{h_m}}$$

↑
diffusive

↑
convective
mass transfer

← denominator
is the total
mass transfer
resistance eq.

$$J_B = \frac{\frac{C_A S D_A}{D_A + Hk} \left(\frac{k}{D_B}\right) \left(\frac{D_B}{h_m} + H\right)}{\left(\frac{H}{D_B} + \frac{1}{h_m}\right)}$$

$$= \frac{\frac{C_A S D_A}{D_A + Hk} k \left(\frac{\cancel{1}}{\cancel{h_m}} + \frac{H}{D_B}\right)}{\left(\frac{\cancel{1}}{\cancel{h_m}} + \frac{H}{D_B}\right)}$$

$$J_B = \frac{C_A S D_A}{D_A + Hk} k$$

(e) As $k \rightarrow 0$, $C_A \rightarrow C_{A0}$ throughout the film
system becomes rate-limited.

$$C_A(x=0) \rightarrow C_{A0}$$

$C_B \rightarrow C_{B0}$ since no reaction
at the interface

As $k \rightarrow \infty$, system becomes diffusion limited for A

$$C_A(x=0) \rightarrow 0$$

Max. possible flux at the interface

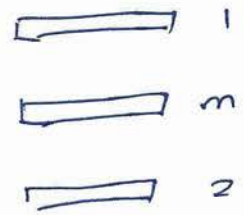
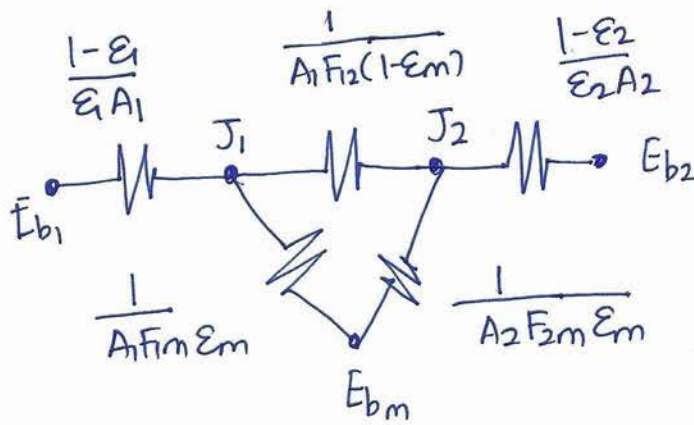
$$J_{A,max} = \frac{D_A C_{A0}}{H}$$

Flux of B will match flux of A.

Diffusion of B will also limit the system.

Q4

(a)



$$\epsilon_1 = 0.4$$

$$\epsilon_m = 0.7$$

$$\epsilon_2 = 0.6$$

$$\tau_m = 0.3$$

(b) Since all plates are long and are in an insulation enclosure, view factors for all are unity.

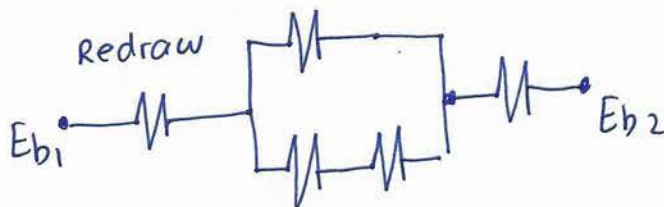
$$F_{12} = 1.0$$

$$F_{1m} = 1.0$$

$$F_{2m} = 1.0$$

$$\text{Also } A_1 = A_2 = A = 0.25 \text{ m}^2$$

(c) Total effective radiation resistance between the top and bottom plate



$$\frac{1}{R_{\text{parallel}}} = \frac{1}{\frac{1}{A_1(1-\epsilon_m)}} + \frac{1}{\frac{2}{A_1\epsilon_m}}$$

$$A_1 = A_2 = A$$

$$= A \left(1 - \frac{\epsilon_m}{2} \right)$$

$$R_{\text{parallel}} = \frac{1}{A \left(1 - \frac{\epsilon_m}{2} \right)} = \frac{1}{0.25(1-0.35)} = 6.154 \text{ m}^{-2}$$

$$\begin{aligned}
 \text{Total } R &= \frac{1-\epsilon_1}{\epsilon_1 A} + 6.154 + \frac{1-\epsilon_2}{\epsilon_2 A} \\
 &= \frac{0.6}{0.4(0.25)} + 6.154 + \frac{0.4}{0.6(0.25)} \\
 &= 14.82 \text{ m}^{-2}
 \end{aligned}$$

d) $E_{b1} = \sigma T_1^4 = 117573 \text{ W/m}^2$
 $E_{b2} = \sigma T_2^4 = 3543.75 \text{ W/m}^2$

looking at the circuit

$$\frac{J_1 - E_{bm}}{1/A\epsilon_m} + \frac{J_2 - E_{bm}}{1/A\epsilon_m} = 0$$

$$1/A\epsilon_m = \frac{1}{0.25(0.7)} = 5.7143$$

$$\boxed{E_{bm} = \frac{J_1 + J_2}{2}}$$

Node J_1

$$\frac{E_{b1} - J_1}{\frac{1-\epsilon_1}{\epsilon_1 A}} = \frac{J_1 - E_{bm}}{\frac{1}{A\epsilon_m}} + \frac{J_1 - J_2}{\frac{1}{A(1-\epsilon_m)}}$$

$$\frac{E_{b1} - J_1}{6} = \frac{J_1 - \left(\frac{J_1 + J_2}{2}\right)}{5.7143} + \frac{J_1 - J_2}{13.333}$$

$$\frac{117573 - J_1}{6} = \frac{J_1 - J_2}{11.43} + \frac{J_1 - J_2}{13.333}$$

$$117573 - J_1 = 0.975(J_1 - J_2)$$

$$117573 = 1.975J_1 - 0.975J_2 \quad \dots \textcircled{1}$$

Node 2

$$\frac{E_{b2} - J_2}{\frac{1 - \epsilon_2}{\epsilon_2 A}} = \frac{J_2 - E_{bm}}{\frac{1}{A \epsilon_m}} + \frac{J_2 - J_1}{\frac{1}{A(1 - \epsilon_m)}}$$

$$\frac{3543.75 - J_2}{2.667} = \frac{J_2 - \left(\frac{J_1 + J_2}{2}\right)}{5.7143} + \frac{J_2 - J_1}{13.333}$$

$$3543.75 - J_2 = -0.4333(J_1 - J_2)$$

$$3543.75 = -0.4333J_1 + 1.4333J_2 \quad \dots \textcircled{2}$$

Solve simultaneous Eqⁿ

$$J_2 = 24060$$

$$J_1 = 71408$$

$$E_{bm} = 47734 \text{ W/m}^2 = \sigma T_m^4$$

$$T_m^4 = 8.42 \times 10^{11}$$

$$\boxed{T_m \approx 958 \text{ K}}$$

(e) $Q_{1 \rightarrow 2} = ?$

$$R_{\text{total}} = 14.82 \text{ m}^{-2}$$

$$Q_{1 \rightarrow 2} = \frac{E_{b1} - E_{b2}}{R_{tot}}$$

$$= \frac{117573 - 3543.75}{14.82}$$

$$= 7694 \text{ W}$$

- (f) Equivalent circuit replaced by a series of R
 "No transmissivity resistor in the circuit
 Since this is an opaque shield, $Q_{1 \rightarrow 2}$ decreases

$$T = \frac{3}{2} \frac{U_b G}{\lambda} \left(\frac{y^2}{2} - \frac{y^4}{12H^2} \right) + T_0$$

let's express the T to include q_w

$$-\lambda \frac{\partial T}{\partial y} \Big|_{y=H} = \dot{q}_w$$

$$-\lambda \frac{\rho C}{\lambda} \frac{3}{2} U_b G \left(H - \frac{H^3}{3H^2} \right) = \dot{q}_w$$

$$\dot{q}_w = -U_b G \rho C H$$

$$U_b G = -\frac{\dot{q}_w}{\rho C H}$$

$$\therefore T = -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(\frac{y^2}{2} - \frac{y^4}{12H^2} \right) + T_0$$

(e) Bulk mean temp

$$T_m = T_0 - \frac{\dot{q}_w H}{2\lambda}$$

velocity-weighted
average temperature

- allows us to find Nu

$$T(y=H) = -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(\frac{H^2}{2} - \frac{H^2}{12} \right) + T_0 \quad \cancel{T(y=H) = T_m}$$

$$= -\frac{3}{2} \frac{\dot{q}_w}{H\lambda} \left(H^2 \frac{5}{12} \right) + T_0$$

$$= -\frac{\dot{q}_w}{\lambda} \frac{5}{8} H + T_0$$

$$T_m = T_0 - \frac{\dot{q}_w H}{\lambda} \frac{39}{280}$$

Heat transfer coefficient

$$h = \frac{\dot{q}_w}{|T_{\text{wall}} - T_m|}$$

$$h = \frac{\dot{q}_w}{|T(y=H) - T_m|}$$

$$h = \frac{\dot{q}_w}{0.486 \dot{q}_w H / \lambda} = \frac{\lambda}{0.486 H}$$

$$Nu = \frac{hD}{\lambda} = \frac{h(2H)}{\lambda}$$

$$= \frac{2}{0.486}$$

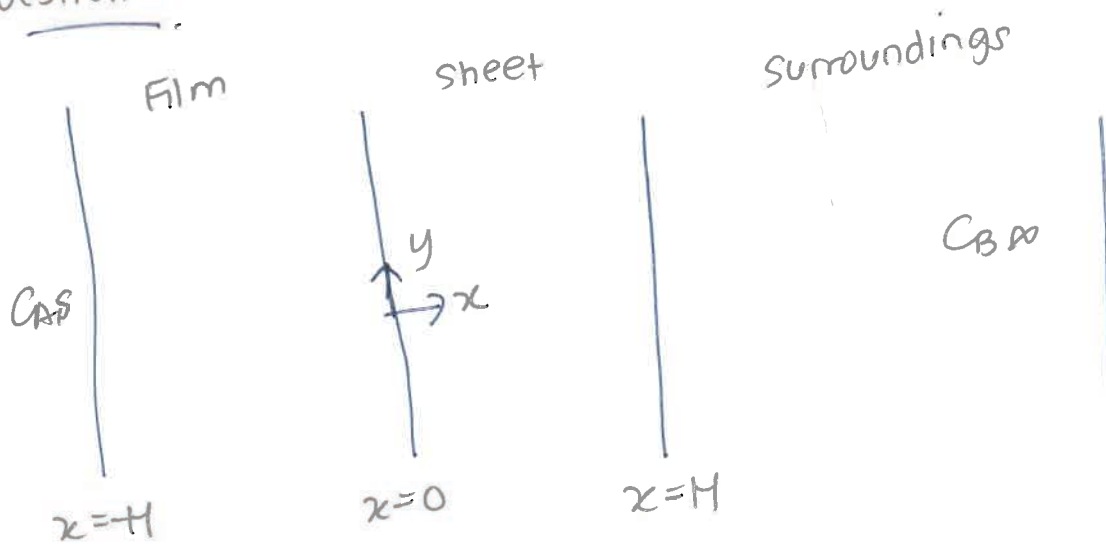
$$= 4.16$$

(f) Higher Nu number near the entrance.

Only a thin layer of fluid near the wall is heated

$(T_{\text{wall}} - T_m) \sim \text{small}$, so $Nu \uparrow$

Question 4



(a) Species A in Film only

$$D \frac{\partial^2 C_A}{\partial x^2} = 0$$

Species B in sheet only

$$D_B \frac{\partial^2 C_B}{\partial x^2} = 0$$

1-D problem

Boundary conditions

(1) $C_A(x = -H) = C_{AS}$

(2) At the film and sheet interface $x = 0$

$$+D_A \left. \frac{\partial C_A}{\partial x} \right|_{x=0} = -k C_A(x=0)$$

(3) $-D_B \left. \frac{\partial C_B}{\partial x} \right|_{x=0} = k C_A(x=0)$

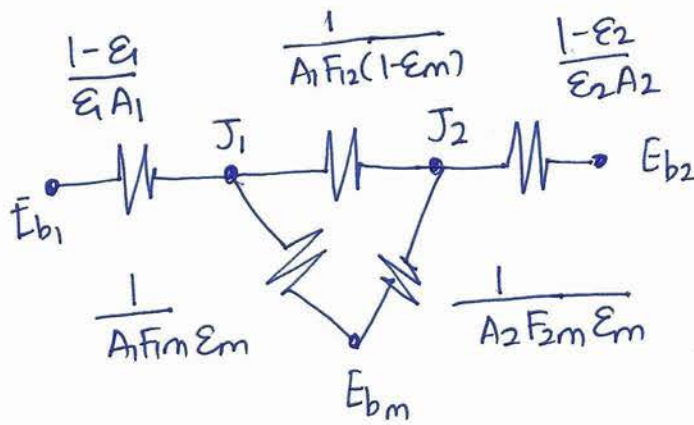
(4) Sheet to surrounding for B

$$-D_B \left. \frac{\partial C_B}{\partial x} \right|_{x=H} = h_m (C_B(x=H) - C_{B\infty})$$

Step 1 Solve $C_A(x)$

Q.2

(a)



$$\epsilon_1 = 0.4$$

$$\epsilon_m = 0.7$$

$$\epsilon_2 = 0.6$$

$$\tau_m = 0.3$$

(b) Since all plates are long and are in an insulation enclosure, view factors for all are unity.

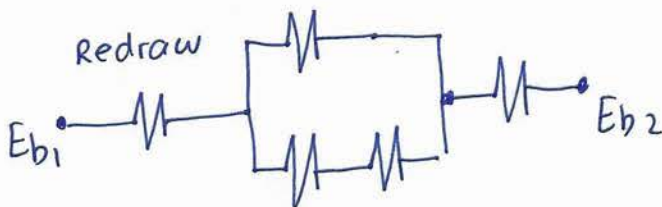
$$F_{12} = 1.0$$

$$F_{1m} = 1.0$$

$$F_{2m} = 1.0$$

$$\text{Also } A_1 = A_2 = A = 0.25 \text{ m}^2$$

(c) Total effective radiation resistance between the top and bottom plate



$$\frac{1}{R_{\text{parallel}}} = \frac{1}{\frac{1}{A_1(1-\epsilon_m)}} + \frac{1}{\frac{2}{A_1\epsilon_m}}$$

$$= A \left(1 - \frac{\epsilon_m}{2} \right)$$

$$A_1 = A_2 = A$$

$$R_{\text{parallel}} = \frac{1}{A \left(1 - \frac{\epsilon_m}{2} \right)} = \frac{1}{0.25(1-0.35)} = 6.154 \text{ m}^{-2}$$