

EGT2
ENGINEERING TRIPOS PART IIA

Tuesday 28 April 2026 14.00 to 15.40

Module 3C8

MACHINE DESIGN

*Answer not more than **three** questions.*

All questions carry the same number of marks.

*The **approximate** percentage of marks allocated to each part of a question is indicated in the right margin.*

*Write your candidate number **not** your name on the cover sheet.*

STATIONERY REQUIREMENTS

Single-sided script paper

SPECIAL REQUIREMENTS TO BE SUPPLIED FOR THIS EXAM

CUED approved calculator allowed

Attachment: Module 3C8 data sheet (9 pages).

Engineering Data Book

10 minutes reading time is allowed for this paper at the start of the exam.

You may not start to read the questions printed on the subsequent pages of this question paper until instructed to do so.

You may not remove any stationery from the Examination Room.

1 Figure 1 shows a diagrammatic side view of a railway locomotive, not drawn to scale. Wheels labelled as D are wheels which are driven by the locomotive's drive system. Wheels labelled as C are wheels which are not driven. The locomotive runs on horizontal track, no braking is considered, and the propelling force is only used to overcome drag forces on the locomotive and to accelerate it.

The locomotive has a mass of 98 tonnes, which is carried evenly by all twelve wheels. All the wheels have a diameter $d = 1.1$ m (taken at the wheel contact surfaces).

Figure 2 shows one pair of wheels on their axle, not drawn to scale. The half-cone angle of the wheels is 2° , as shown. Each wheel runs on a rail. A cross-sectional view of the right-hand rail is included in the figure. The radius on the top of each rail-head, where the wheels contact, is $R_w = 0.3$ m.

The wheels and rails are made of steel, with contact modulus $E^* = 115$ GPa and Poisson's ratio $\nu = 0.3$. For the purposes of identifying the Hertz contact geometry, the wheel should be taken to be locally cylindrical at the point of contact.

- (a) Determine the Hertz contact pressure at each wheel-rail contact. [10%]
- (b) Determine the surface deflections of the wheel and rail at each wheel-rail contact. [10%]
- (c) Stating any assumptions made, determine the maximum subsurface shear stress at each wheel-rail contact. [10%]
- (d) Find the depth at which the maximum shear stress occurs in the wheels and rails. [10%]
- (e) Estimate the efficiency with which the power that the locomotive transmits to the wheels is available to drive the railway locomotive along the track (i.e. to overcome external drag and to accelerate the locomotive). Assume that the drive forces are 75% of their limiting value and that the contact patch is circular. [40%]
- (f) Find the shapes, sizes and orientations of the contact patches, stating any assumptions made. Calculate the spin pole offset for the two different wheel types, showing the spin pole locations on sketches of the contact patches. [20%]

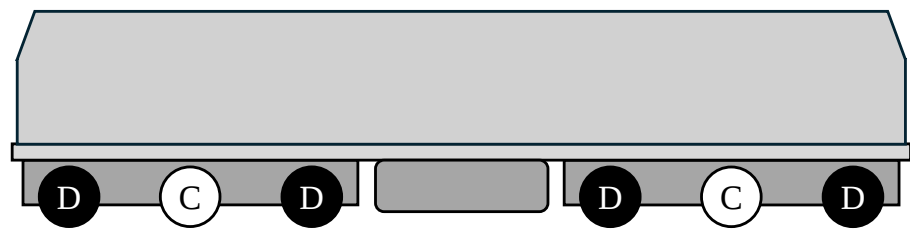


Fig. 1

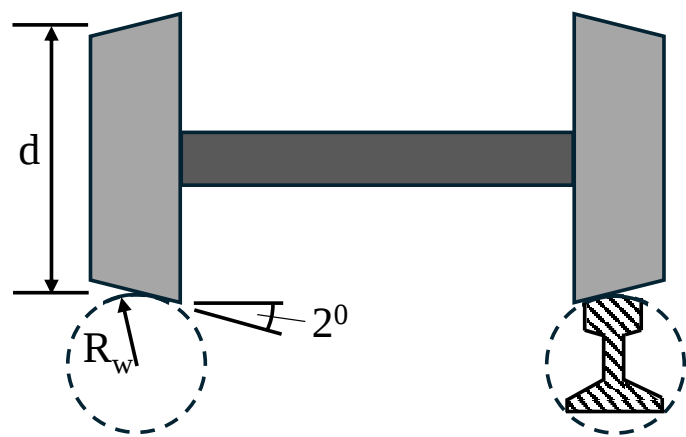


Fig. 2

2 The output characteristic of a bicycle rider working at their full effort is shown in Fig. 3, where the mean torque T applied to the crank by the rider depends linearly on the angular speed ω of the crank. The intercepts on the axes are $T_0 = 60 \text{ N m}$ and $\omega_0 = 20 \text{ rad s}^{-1}$.

(a) Derive an expression for the mean crank output power P as a function of crank angular speed ω . Sketch P versus ω . Mark the mean crank torque and crank angular speed corresponding to the maximum crank output power on your sketch. [20%]

(b) The ratio of the wheel angular speed Ω to the crank angular speed ω is given by $G = \Omega/\omega$. The rider and bicycle have a total mass $m = 100 \text{ kg}$, frontal area $A = 0.5 \text{ m}^2$, aerodynamic drag coefficient $C_d = 0.8$, and wheel radius $r = 0.35 \text{ m}$. The force F (in N) resisting forward motion at constant speed V is:

$$F = mg\alpha + 0.5\rho C_d A V^2$$

where g is the gravitational acceleration (take $g = 10 \text{ m s}^{-2}$), $\rho = 1.2 \text{ kg m}^{-3}$ is the air density and α is the gradient of the road (in radians).

The rider and bicycle travel from home to work over a route of 10 km. The route can be modelled as two consecutive stages of 5 km. The first 5 km have zero gradient (i.e. level), and the second 5 km have a constant gradient of $\alpha = 0.05$ (i.e. uphill). The transient acceleration at the beginning of each stage can be ignored. Find the speed ratio G_1 required to complete the first stage in minimum time. Find the speed ratio G_2 required to complete the second stage in minimum time. Hence find the minimum total time to travel the 10 km route. [30%]

(c) An electric motor is installed on the bicycle, such that the torque T_M delivered by the motor is applied directly to the crank shaft. The output characteristics of the electric motor, in terms of T_M as a function of crank angular speed ω , are given in Fig. 4. The rated torque of the motor is 20 N m. State the definition of the rated torque for an electric motor, and discuss the implications of generating torque in excess of the rated torque. [10%]

(d) The motor controller limits the motor torque to be no greater than the rated torque over the operating range shown in Fig. 4. Find the maximum acceleration that the rider and bicycle can achieve on level ground with $G = 1.1$. The weight increase due to the motor can be ignored. [20%]

(e) The rider and bicycle cruise at a constant speed $V_0 = 10 \text{ m s}^{-1}$ on a level road. The rider then chooses to coast (i.e. no pedalling and no motor torque). Derive the speed of the rider and bicycle as a function of time during coasting. Estimate the distance that the rider and the bicycle have coasted for when the speed drops to 3 m s^{-1} .

[20%]

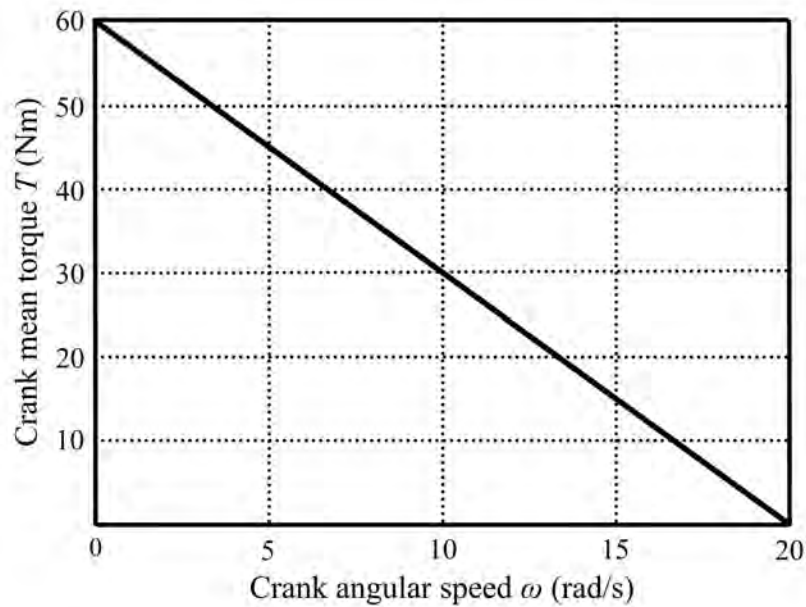


Fig. 3

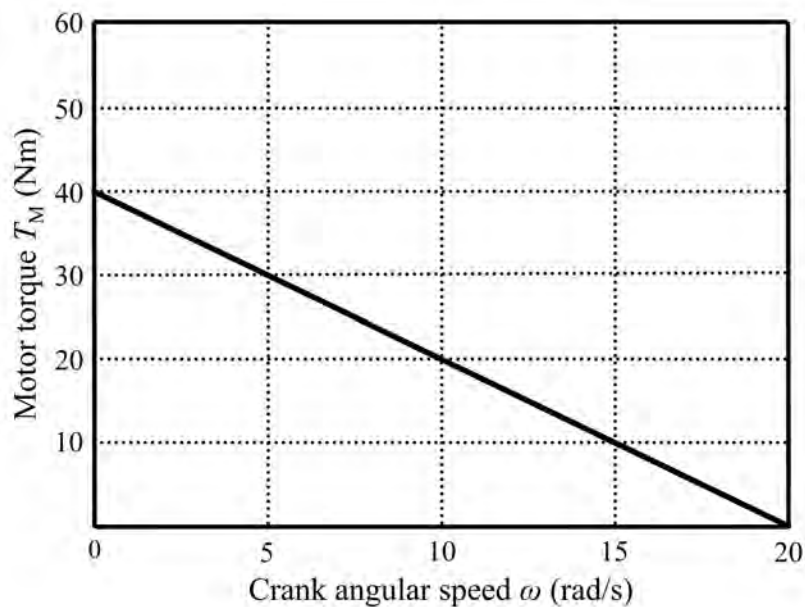


Fig. 4

3 (a) A rotating shaft is supported within a stationary housing by rolling-element bearings. The shaft is required to carry both radial and axial loads.

(i) It has been determined that the shaft can be supported using three bearings: two cylindrical roller bearings to support radial forces only and one deep groove ball bearing to support axial forces only. Sketch a suitable conceptual arrangement of the assembly showing the fundamental geometry of the shaft and the housing. Clearly show the interfaces between the bearings, the shaft and the housing, and clearly indicate where clearances exist. [15%]

(ii) Explain how thermal expansion of the shaft may be accommodated. [10%]

(iii) It is proposed to use cylindrical roller bearing NU310EC in the design. In the condition of ideal lubrication for the bearing, calculate the allowable radial force acting on the bearing for a life of 20,000 revolutions with 99% reliability. Comment on the value of this force in relation to the static load rating of the bearing. [15%]

(iv) It is proposed to replace the deep groove ball bearing in the current design with a double-row angular contact ball bearing. Discuss the implications of this replacement. [10%]

(b) Figure 5 illustrates a gearbox. The sun input shaft rides freely on the carrier input shaft, and both these input shafts and the output shaft run in bearings in the casing. Planet gears B and D are rigidly connected to each other and run on a bearing within the carrier. Losses in the gearbox and bearings may be neglected. Tooth numbers for gears A, B, D and E are denoted by their respective labels (A, B, D and E). The input torques on the carrier and sun are T_C and T_S respectively and the torque acting on the output shaft is T_O .

Find expressions for the output speed Ω_O and output torque T_O in terms of the carrier input speed Ω_C and torque T_C , and the gear tooth numbers, for the following cases:

(i) $\Omega_S = \Omega_C$; [10%]

(ii) $\Omega_S = 0$; [20%]

(iii) $\Omega_S = -\Omega_C/2$; [20%]

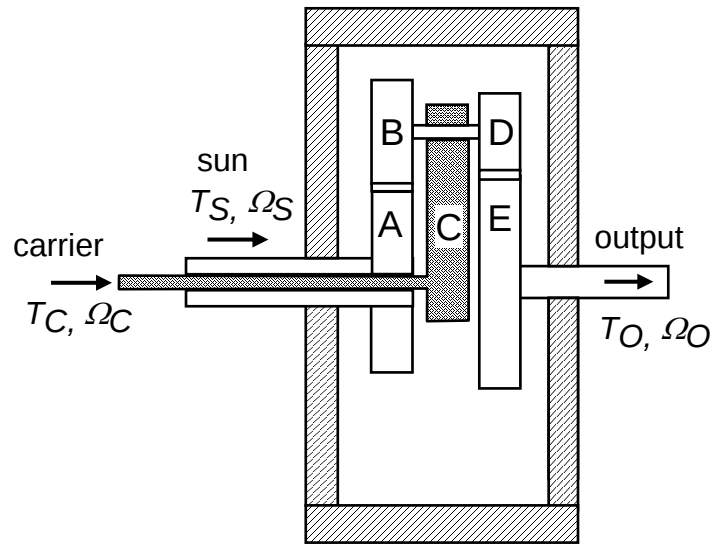


Fig. 5

- 4 (a) Briefly discuss the role of lubrication in gear transmission systems? [10%]
- (b) Outline steps in a simple model to estimate tooth friction losses in involute gears. A detailed derivation is not required. [15%]
- (c) Consider failure of two spur gears. The pinion has 17 teeth and the wheel has 61 teeth. Both gears have standard involute tooth profiles with the addendum a equal to the the module $m = 4$ mm and a pressure angle $\phi = 20^\circ$. The tooth face width is $4m$. The gears are not accurately made, so that load-sharing between teeth cannot be assumed. The gears are made of steel ($E^* = 115$ GPa) with bending and surface fatigue strengths of 300 MPa and 800 MPa, respectively.
- (i) Find the maximum pinion torque before tooth bending failure is expected. [20%]
- (ii) Find the minimum effective radius of curvature for single pair contact. [30%]
- (iii) Find the maximum pinion torque before surface failure is expected. [15%]
- (iv) How would your answers to the above parts (i), (ii) and (iii) change if the module is doubled? [10%]

END OF PAPER

ENGINEERING TRIPOS Part IIA

Module 3C8 Data Sheet

ELASTIC CONTACT STRESS FORMULAE

Suffixes 1, 2 refer to the two bodies in contact.

Effective curvature $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$

Contact modulus $\frac{1}{E^*} = \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}$

where R_1, R_2 are the radii of curvature of the two bodies (convex positive).

where E_1, E_2 and ν_1, ν_2 are Young's moduli and Poisson's ratios

	<u>Line contact</u> width $2b$; load P' per unit length	<u>Circular contact</u> diameter $2a$; load P
Semi contact width or contact radius	$b = 2 \left\{ \frac{P'R}{\pi E^*} \right\}^{1/2}$	$a = \left\{ \frac{3PR}{4E^*} \right\}^{1/3}$
Maximum contact pressure ('Hertz stress')	$p_0 = \left\{ \frac{P'E^*}{\pi R} \right\}^{1/2}$	$p_0 = \frac{1}{\pi} \left\{ \frac{6PE^{*2}}{R^2} \right\}^{1/3}$
Approach of centres	$\delta = \frac{2P'}{\pi} \left[\frac{1 - \nu_1^2}{E_1} \left\{ \ln \left(\frac{4R_1}{b} \right) - \frac{1}{2} \right\} + \frac{1 - \nu_2^2}{E_2} \left\{ \ln \left(\frac{4R_2}{b} \right) - \frac{1}{2} \right\} \right]$	$\delta = \frac{a^2}{R} = \frac{1}{2} \left\{ \frac{9}{2} \frac{P^2}{E^{*2} R} \right\}^{1/3}$
Mean contact pressure	$\bar{p} = \frac{P'}{2b} = \frac{\pi}{4} p_0$	$\bar{p} = \frac{P}{\pi a^2} = \frac{2}{3} p_0$
	$\tau_{\max} = 0.300 p_0$ at $x = 0, z = 0.79b$	$\tau_{\max} = 0.310 p_0$ at $r = 0, z = 0.48a$ for $\nu = 0.3$
Maximum tensile stress	zero	$\frac{1}{3}(1 - 2\nu)p_0$ at $r = a, z = 0$

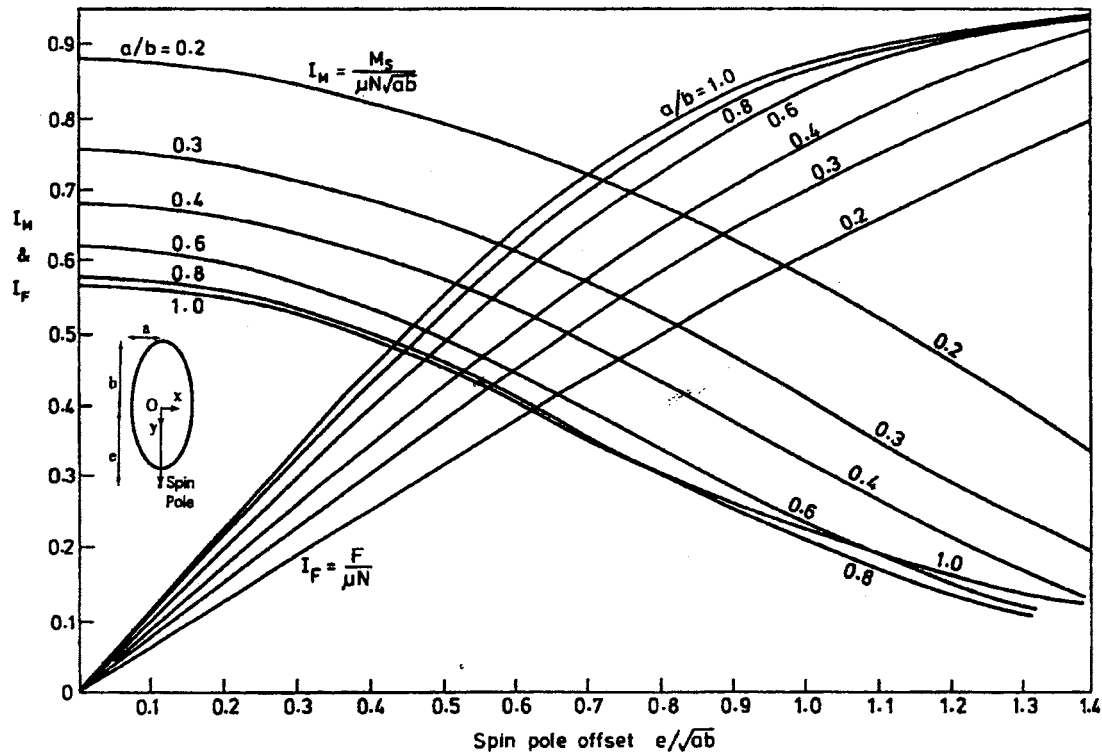
Mildly elliptical contacts

If the gap at zero load is $h = \frac{1}{2}Ax^2 + \frac{1}{2}By^2$ and $0.2 < A/B < 5$ then
ratio of semi-axes $b/a \equiv (A/B)^{2/3}$

To calculate the contact **area** or Hertz **stress** use the circular contact equations with $R = (AB)^{-1/2}$ or better $R_e = [AB(A + B)/2]^{-1/3}$.

For **approach** use circular contact equation with $R = (AB)^{-1/2}$ (**not** R_e)

Hertzian contact frictional losses

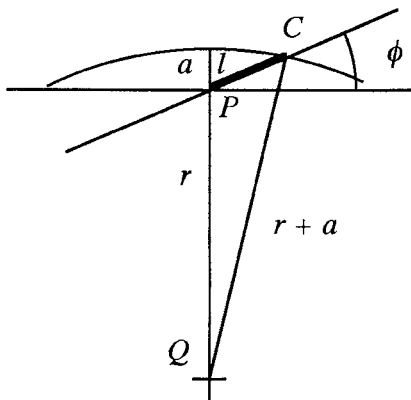


INVOLUTE GEARING

Spur gears

pitch cylinder radii	r	} with suffix 1 or 2	circumferential pitch	$p = 2\pi r/N$
base cylinder radii	r_b		base pitch	$p_b = p \cos \phi$
addendum cylinder radii	r_a		module	$m = p/\pi = 2r/N$
number of teeth	N		ratio of contact	r_c
addendum	$a = r_a - r$		radius of curvature at pitch point	$\rho = r \sin \phi$
pressure angle	ϕ			

Path of contact



$$l = \left\{ r^2 \sin^2 \phi + a(2r + a) \right\}^{1/2} - r \sin \phi$$

For a standard 20° spur wheel with N teeth of module m this becomes

$$\frac{l}{m} = \left(0.02924N^2 + N + 1 \right)^{1/2} - 0.1710N$$

Standard tooth forms

Addendum $a = m$, Dedendum $= \frac{7}{6}m$, pressure angle $= 20^\circ$.

Modules:

	0.3 – 1.0 mm in 0.1 mm steps
1.0 – 4.0 mm in 0.25 mm steps	4.0 – 7.0 mm in 0.5 mm steps
7.0 – 16.0 mm in 1.0 mm steps	16.0 – 24.0 mm in 2.0 mm steps
24.0 – 45.0 mm in 3.0 mm steps	45.0 – 75.0 mm in 5.0 mm steps

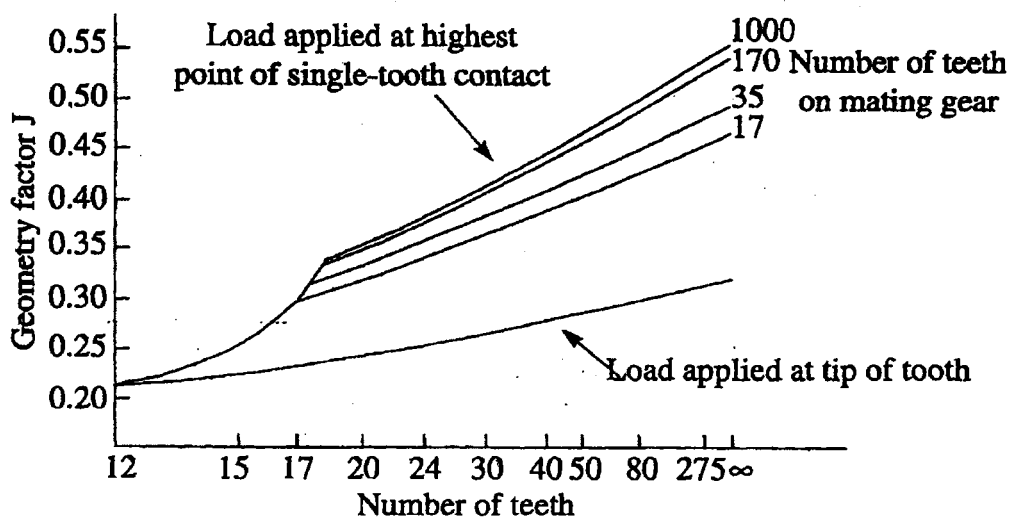
Friction in spur gears

$$\frac{\text{average friction loss}}{\text{power transmitted}} \approx \mu\pi \left\{ \frac{1}{N_1} + \frac{1}{N_2} \right\}$$

Tooth failure

Allowable bending stress σ_b according to AGMA guidelines given by $\sigma_b = \frac{P'_T}{Jm}$

where P'_T is force per unit face-width acting tangentially to pitch circle and J given in the figure below for 20° spur gears. Typical values of σ_b shown in table.



Typical allowable tooth stresses (AGMA)

Material	Condition	Bending fatigue strength σ_b (MPa)	Surface fatigue strength σ_s (MPa)
Steel	Through hardened and tempered	170-390	590-1200
	Carburised and case hardened	380-480	1250-1550
Cast iron	As cast	69-90	450-590
Nodular iron	Quenched, annealed and tempered	150-300	500-800
Malleable iron	Pearlitic	70-145	500-650

EPICYCLIC SPEED RULE

$$\omega_s = (1 + R)\omega_c - R\omega_a \quad \text{where } R = \frac{A}{S}$$

ROLLING ELEMENT BEARINGS

Fatigue life

$$L = a_1 a_{23} (C/P)^p \quad p = 3 \text{ for ball and } 10/3 \text{ for roller bearings}$$

Fatigue probability %	10	5	4	3	2	1
Life adjust factor a_1	1	0.62	0.53	0.44	0.33	0.21

Bearing choice

The information on the following pages concerning loads, viscosities and standard bearing sizes and ratings is extracted from the SKF General Bearing Catalogue and is copied with permission. It is SKF copyright and is not to be further reproduced.

MPFS, DJC, JAW
September 2021

Required viscosities and the effect of viscosity ratio on a_{23}

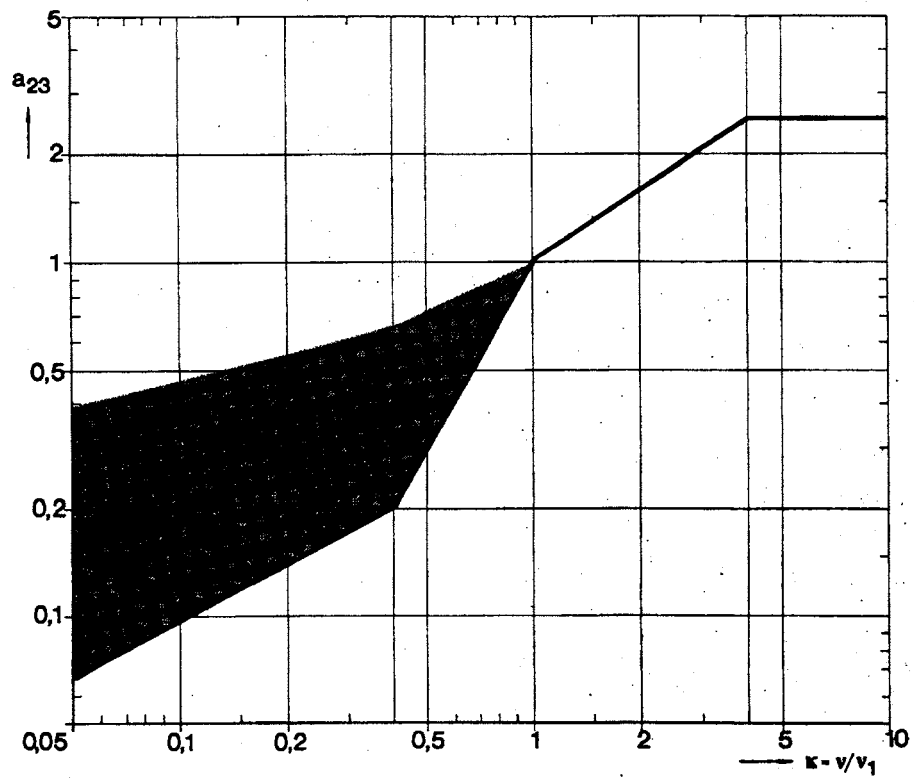
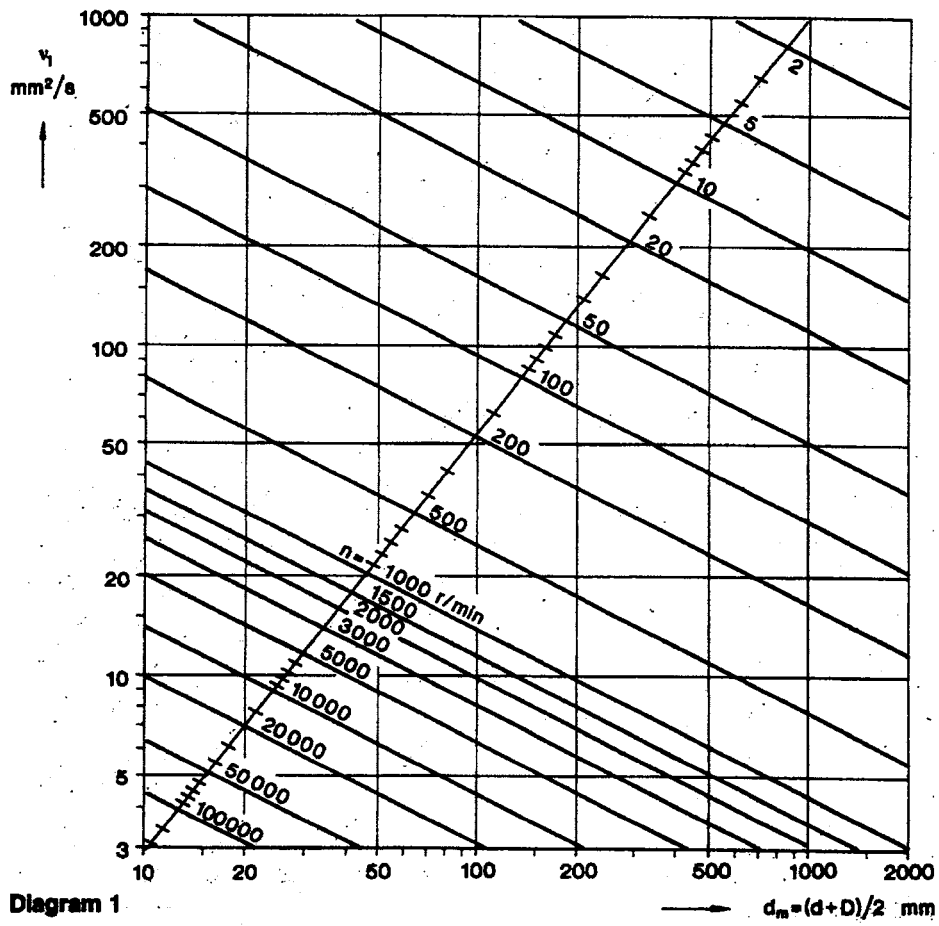
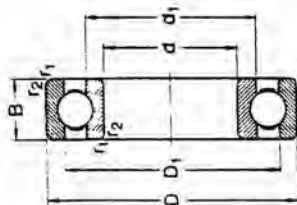
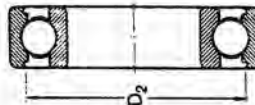


Diagram 3

Deep groove ball bearings
single row
d 35–55 mm



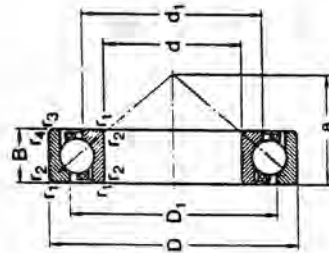
With full outer
ring shoulders



With recessed outer
ring shoulders

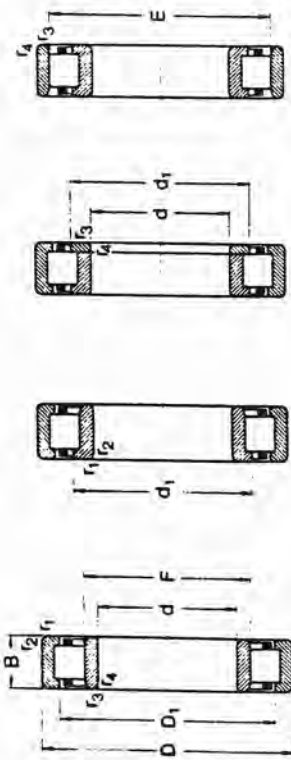
Principal dimensions			Basic load ratings			Fatigue load limit		Speed ratings		Mass		Designation	
d	D	B	C	C ₀	P ₀	N	r/min	kg					
35	47	7	4 750	3 200	166	13 000	16 000	0.030	61807				
55	55	10	9 560	6 200	290	11 000	14 000	0.080	61907				
62	72	14	12 400	8 150	375	10 000	13 000	0.11	6007				
62	72	14	15 900	10 200	440	9 000	11 000	0.16	6207				
72	80	16	25 500	15 300	655	8 500	10 000	0.29	6307				
80	90	18	32 200	19 000	815	7 000	8 500	0.46	6407				
100	110	25	55 300	31 000	1 290	5 000	6 000	0.95	6807				
40	52	7	4 940	3 450	186	11 000	14 000	0.034	61808				
52	62	12	13 800	9 300	425	10 000	13 000	0.12	61908				
68	78	16	20 800	13 500	680	9 500	12 000	0.19	6008				
68	78	16	25 500	16 000	815	8 500	10 000	0.37	6208				
80	90	18	30 700	19 000	1 020	7 500	9 000	0.63	6308				
90	100	23	41 000	24 000	1 340	6 000	7 000	1.25	6408				
110	120	27	63 700	36 500	1 530	5 000	6 000	2.30	6808				
45	58	7	6 050	4 300	228	9 500	12 000	0.040	61809				
58	68	12	10 100	6 700	285	8 500	11 000	0.14	61909				
68	78	16	15 600	10 800	440	7 500	9 000	0.25	6009				
75	85	18	20 800	14 800	640	6 500	8 000	0.41	6209				
85	95	20	33 200	21 600	915	5 500	6 500	0.83	6309				
100	110	25	52 700	31 500	1 340	4 500	5 500	1.55	6409				
120	140	33	76 100	45 000	1 900	3 500	4 500	3.30	6809				
50	65	7	6 240	4 750	250	9 000	11 000	0.052	61810				
72	80	12	14 600	10 400	500	8 500	10 000	0.14	61910				
80	90	16	21 600	15 000	710	7 500	9 000	0.26	6010				
80	90	16	25 500	16 000	815	6 500	8 000	0.48	6210				
90	100	20	35 100	23 200	960	5 500	6 500	1.05	6310				
110	120	27	61 800	38 000	1 600	4 500	5 500	2.30	6410				
130	150	31	87 100	52 000	2 200	3 500	4 500	4.00	6810				
55	72	9	8 320	6 200	325	8 500	10 000	0.083	61811				
72	80	12	15 900	11 400	560	7 500	9 000	0.19	61911				
80	90	16	21 600	15 000	710	6 500	8 000	0.26	6011				
80	90	16	25 500	16 000	815	5 500	6 500	0.39	6211				
90	100	20	35 100	23 200	960	4 500	5 500	0.61	6311				
110	120	27	61 800	38 000	1 600	3 500	4 500	1.35	6411				
130	150	31	87 100	52 000	2 200	2 500	3 500	2.30	6811				

Angular contact ball bearings
single row
d 10–65 mm



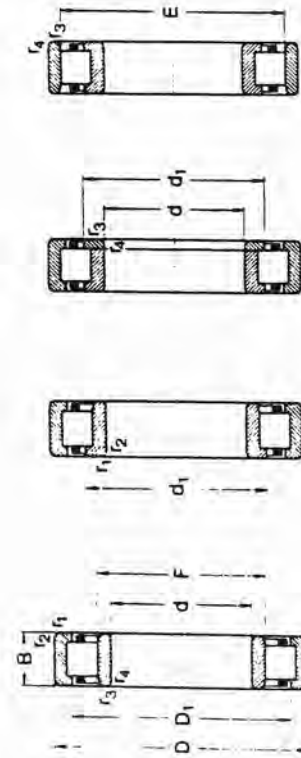
Principal dimensions			Basic load ratings			Fatigue load limit		Speed ratings		Mass		Designation	
d	D	B	C	C ₀	P ₀	N	r/min	kg					
10	30	9	7 020	3 350	140	19 000	28 000	0.030	7200 BE				
12	32	10	7 610	3 800	160	18 000	26 000	0.036	7201 BE				
15	35	11	8 840	4 800	204	17 000	24 000	0.045	7202 BE				
17	40	12	11 100	6 100	260	15 000	20 000	0.065	7203 BE				
20	47	14	14 000	8 300	355	12 000	17 000	0.11	7204 BE				
25	52	15	15 600	10 200	430	10 000	15 000	0.13	7205 BE				
30	62	17	23 800	15 600	655	8 500	12 000	0.20	7206 BE				
35	72	19	30 700	20 800	880	8 000	11 000	0.28	7207 BE				
40	80	18	36 400	26 000	1 100	7 000	9 500	0.37	7208 BE				
45	85	19	37 700	28 000	1 200	6 700	9 000	0.42	7209 BE				
50	90	20	39 000	30 500	1 280	6 000	8 000	0.47	7210 BE				
55	100	21	48 800	38 000	1 630	5 500	7 500	0.62	7211 BE				
60	110	22	57 200	45 500	1 930	5 000	6 700	0.80	7212 BE				
65	120	23	66 300	54 000	2 280	4 500	6 000	1.00	7213 BE				

Cylindrical roller bearings single row d 50–55 mm



Principal dimensions	Type NU			Type NUP			Type N		
	d	D	B	C	C ₀	Fatigue load limit P _u	Speed ratings Lubrication grease oil	Mass	Designation
	mm			N			r/min		
50	80	16	30	800	34 500	4 000	8 500	10 000	NU 1010
	90	20	64	400	69 500	8 800	6 300	7 500	NU 210 EC
	90	20	64	400	69 500	8 800	6 300	7 500	NJ 210 EC
	90	20	64	400	69 500	8 800	6 300	7 500	NUP 210 EC
	90	20	64	400	69 500	8 800	6 300	7 500	N 210 EC
	90	23	78	100	88 000	11 400	6 300	7 500	NU 2210 EC
	90	23	78	100	88 000	11 400	6 300	7 500	NJ 2210 EC
	90	23	78	100	88 000	11 400	6 300	7 500	NUP 2210 EC
	110	27	110	000	112 000	15 000	5 000	6 000	NU 310 EC
	110	27	110	000	112 000	15 000	5 000	6 000	NJ 310 EC
	110	27	110	000	112 000	15 000	5 000	6 000	NUP 310 EC
	110	27	110	000	112 000	15 000	5 000	6 000	N 310 EC
	110	40	161	000	186 000	24 500	5 000	6 000	NU 2310 EC
	110	40	161	000	186 000	24 500	5 000	6 000	NJ 2310 EC
	110	40	161	000	186 000	24 500	5 000	6 000	NUP 2310 EC
	130	31	130	000	127 000	16 600	5 000	6 000	NU 410
	130	31	130	000	127 000	16 600	5 000	6 000	NJ 410
55	90	18	57	200	69 500	8 300	7 000	8 500	NU 1011 EC
	100	21	84	200	95 000	12 200	6 000	7 000	NU 211 EC
	100	21	84	200	95 000	12 200	6 000	7 000	NJ 211 EC
	100	21	84	200	95 000	12 200	6 000	7 000	NUP 211 EC
	100	21	84	200	95 000	12 200	6 000	7 000	N 211 EC
	100	25	99	000	118 000	15 300	6 000	7 000	NU 2211 EC
	100	25	99	000	118 000	15 300	6 000	7 000	NJ 2211 EC
	100	25	99	000	118 000	15 300	6 000	7 000	NUP 2211 EC
	100	25	99	000	118 000	15 300	6 000	7 000	N 2211 EC
	120	29	138	000	143 000	18 600	4 800	5 600	NU 311 EC
	120	29	138	000	143 000	18 600	4 800	5 600	NJ 311 EC
	120	29	138	000	143 000	18 600	4 800	5 600	NUP 311 EC
	120	29	138	000	143 000	18 600	4 800	5 600	N 311 EC

Cylindrical roller bearings single row d 40–45 mm

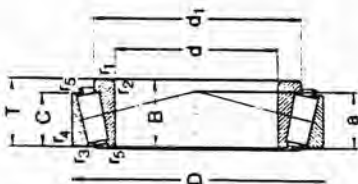


Principal dimensions	Type NU			Type NUP			Type N		
	d	D	B	C	C ₀	Fatigue load limit P _u	Speed ratings Lubrication grease oil	Mass	Designation
	mm			N			r/min		
40	90	23	80	900	78 000	10 200	6 700	8 000	NU 308 EC
(cont.)	90	23	80	900	78 000	10 200	6 700	8 000	NJ 308 EC
	90	23	80	900	78 000	10 200	6 700	8 000	NUP 308 EC
	90	23	80	900	78 000	10 200	6 700	8 000	N 308 EC
	90	33	112	000	120 000	15 300	6 300	7 500	NU 2308 EC
	90	33	112	000	120 000	15 300	6 300	7 500	NJ 2308 EC
	90	33	112	000	120 000	15 300	6 300	7 500	NUP 2308 EC
	110	27	96	800	90 000	11 600	6 000	7 000	NU 408
	110	27	96	800	90 000	11 600	6 000	7 000	NJ 408
	110	27	96	800	90 000	11 600	6 000	7 000	NUP 408
45	75	16	44	600	52 000	6 300	9 000	11 000	NU 1008 EC
	85	19	60	500	64 000	8 150	6 700	8 000	NU 208 EC
	85	19	60	500	64 000	8 150	6 700	8 000	NJ 208 EC
	85	19	60	500	64 000	8 150	6 700	8 000	NUP 208 EC
	85	19	60	500	64 000	8 150	6 700	8 000	N 208 EC
	85	23	73	700	81 500	10 600	6 700	8 000	NU 2208 EC
	85	23	73	700	81 500	10 600	6 700	8 000	NJ 2208 EC
	85	23	73	700	81 500	10 600	6 700	8 000	NUP 2208 EC
	85	23	73	700	81 500	10 600	6 700	8 000	N 2208 EC
	100	25	99	000	100 000	12 900	6 300	7 500	NU 309 EC
	100	25	99	000	100 000	12 900	6 300	7 500	NJ 309 EC
	100	25	99	000	100 000	12 900	6 300	7 500	NUP 309 EC
	100	25	99	000	100 000	12 900	6 300	7 500	N 309 EC
	100	36	138	000	153 000	20 000	5 600	6 700	NU 2309 EC
	100	36	138	000	153 000	20 000	5 600	6 700	NJ 2309 EC
	100	36	138	000	153 000	20 000	5 600	6 700	NUP 2309 EC
	120	29	106	000	102 000	13 400	5 600	6 700	NU 409
	120	29	106	000	102 000	13 400	5 600	6 700	NJ 409
	120	29	106	000	102 000	13 400	5 600	6 700	NUP 409
	120	29	106	000	102 000	13 400	5 600	6 700	N 409

Taper roller bearings

single row

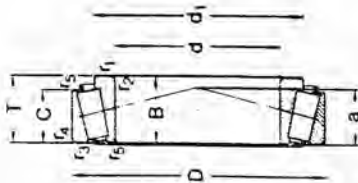
d 50–65 mm



Taper roller bearings

single row

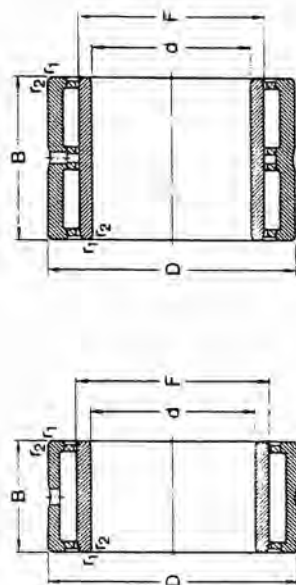
d 35–50 mm



Principal dimensions		Basic load ratings		Speed ratings		Fatigue load limit		Mass		Designation		Dimension Series to ISO 355	
d	D	T	C	C ₀	N	r/min	P _u	N	kg	kg			
50	110	29,25	125 000	140 000	17 000	3 600	4 800	1,25	30310	2FB			
(cont.)	110	29,25	106 000	120 000	14 300	3 200	4 300	1,20	31310	7FB			
	110	42,25	172 000	212 000	24 500	3 200	4 300	1,80	32310	2FD			
	110	42,25	161 000	216 000	25 000	3 200	4 300	1,85	32310 B	5FD			
55	80	23	78 100	112 000	12 500	4 000	5 300	0,56	K-JLM 506849/K-JLM 506810				
	80	23	80 900	116 000	13 200	4 000	5 300	0,55	32011 X	3CC			
	80	27	89 700	137 000	15 300	4 000	5 300	0,67	33011	2CE			
	85	27	110 000	156 000	18 000	3 800	5 000	0,86	33111	3CE			
	100	22,75	89 700	106 000	12 200	3 800	5 000	0,70	32011	3DB			
	100	26,75	106 000	129 000	15 300	3 800	5 000	0,83	32211	3DC			
	100	26,75	101 000	127 000	15 300	3 600	4 800	0,87	32211 B				
	100	35	138 000	190 000	22 000	3 400	4 500	1,20	32111	3DE			
	110	39	178 000	232 000	26 600	3 400	4 500	1,70	T2ED 055	2ED			
	115	34	125 000	163 000	19 600	3 000	4 000	1,55	T7FC 055	7FC			
	120	31,5	142 000	183 000	19 600	3 200	4 300	1,55	30311	2FB			
	120	45,5	121 000	137 000	17 000	2 800	3 800	2,30	31311	7FB			
	120	45,5	188 000	250 000	29 000	3 000	4 000	2,30	32311	2FD			
	120	45,5	190 000	260 000	30 000	2 800	3 800	2,50	32311 B	5FD			
60	95	23	82 500	122 000	13 700	3 800	5 000	0,59	32012 X	4CC			
	95	24	84 200	132 000	15 000	3 600	4 800	0,62	K-JLM 506748/K-JLM 506710				
	95	27	91 300	143 000	16 000	3 800	5 000	0,71	33012	2CE			
	100	30	117 000	170 000	19 600	3 800	4 800	0,92	33112	3CE			
	110	29,75	99 000	114 000	13 400	3 400	4 500	0,86	30212	3EC			
	110	29,75	125 000	160 000	19 000	3 400	4 500	1,15	32212	3EE			
	115	39	168 000	236 000	27 000	3 000	4 000	1,60	33212	3ED			
	115	40	194 000	260 000	27 500	3 200	4 300	1,85	T2ED 060	5ED			
	125	37,5	154 000	204 000	24 500	3 200	4 300	1,85	T5ED 060	2EE			
	130	33,5	168 000	196 000	23 600	2 800	3 800	2,05	T7FC 060	7FC			
	130	33,5	145 000	166 000	20 400	3 000	4 000	1,90	31312	2FB			
	130	48,5	229 000	280 000	34 500	2 800	3 800	2,85	32312	2FD			
	130	48,5	220 000	305 000	35 500	2 600	3 600	2,80	32312 B	5FD			
65	100	23	84 200	127 000	14 300	3 400	4 500	0,63	32013 X	4CC			
	100	27	96 800	156 000	17 600	3 400	4 500	0,78	33013	2CE			
	110	28	123 000	183 000	21 200	3 200	4 300	1,05	K-JLM 511046/K-JLM 511010				
	110	24	142 000	204 000	24 500	3 200	4 300	1,30	32113	3DE			
	120	24,75	111 000	134 000	16 300	3 000	4 000	1,15	30213	3EB			
	120	32,75	151 000	193 000	23 200	3 000	4 000	1,50	32213	3EC			
	120	39	181 000	240 000	27 600	3 000	4 000	1,95	T5ED 065	5ED			

Principal dimensions		Basic load ratings		Speed ratings		Fatigue load limit		Mass		Designation		Dimension Series to ISO 355	
d	D	T	C	C ₀	N	r/min	P _u	N	kg	kg			
35	80	22,75	72 100	73 500	8 500	5 000	6 700	0,52	30307	2FB			
(cont.)	80	22,75	61 600	67 000	7 800	4 500	6 000	0,52	31307	7FB			
	80	32,75	95 200	106 000	12 200	4 800	6 300	0,73	32307	2FE			
	80	32,75	93 500	114 000	13 200	4 500	6 000	0,80	32307 B	5FE			
40	68	19	52 800	71 000	7 800	5 300	7 000	0,27	32008 X	3CD			
	75	26	79 200	104 000	11 600	5 000	6 700	0,51	33108	2CE			
	80	19,75	61 600	68 000	7 650	4 800	6 300	0,42	30208	3DB			
	80	24,75	74 800	86 500	9 800	4 800	6 300	0,53	32208	3DC			
	80	32	105 000	132 000	15 300	4 300	5 600	0,77	33208	2DE			
	85	33	121 000	150 000	17 300	4 500	6 000	0,90	T2EE 040	2EE			
	90	25,25	85 800	95 000	11 000	4 500	6 000	0,72	30308	2FB			
	90	25,25	73 700	81 500	9 650	4 000	5 300	1,00	31308	7FB			
	90	35,25	117 000	140 000	16 300	4 000	5 300	1,00	32308	2FD			
	90	35,25	108 000	140 000	16 300	4 000	5 300	1,10	32308 B	5FD			
45	75	20	58 300	80 000	8 800	4 800	6 300	0,34	32009 X	3CC			
	80	26	66 000	76 500	8 650	4 500	6 000	0,56	33109	3CE			
	85	20,75	66 000	76 500	8 650	4 500	6 000	0,48	30209	3DB			
	85	24,75	80 900	99 000	11 200	4 500	6 000	0,58	32209	3DC			
	85	32	108 000	143 000	16 300	4 300	5 600	0,82	33209	5DC			
	95	29	89 700	112 000	12 900	3 600	4 800	0,82	T7FC 045	7FC			
	95	36	147 000	186 000	21 200	4 000	5 300	1,20	T2ED 045	2ED			
	100	27,25	108 000	120 000	14 600	4 000	5 300	0,97	30309	2FB			
	100	27,25	91 300	102 000	12 500	3 400	4 500	0,85	31309	7FB			
	100	38,25	140 000	170 000	20 400	3 600	4 800	1,35	32309	2FD			
	100	38,25	134 000	176 000	20 000	3 600	4 800	1,45	32309 B	5FD			
50	80	20	60 500	88 000	9 650	4 500	6 000	0,37	32010 X	3CC			
	80	24	69 300	102 000	11 400	4 500	6 000	0,43	33010	2CE			
	82	21,5	72 100	100 000	11 000	4 500	6 000	0,43	K-JLM 104948/K-JLM 104910				
	85	26	85 800	122 000	13 700	4 300	5 600	0,59	33110	3CE			
	90	21,75	76 500	91 500	10 400	4 300	5 600	0,54	30210	3DB			
	90	24,75	82 500	100 000	11 600	4 300	5 600	0,61	32210	3DC			
	90	24,75	82 500	104 000	12 500	4 000	5 300	0,85	32210 B	5DC			
	90	28	105 000	140 000	16 300	4 000	5 300	0,75	K-JLM 205149/K-JLM 205110				
	90	32	114 000	160 000	18 300	4 000	5 300	0,75	K-JLM 205149/K-JLM 205110 A				
	90	32	114 000	160 000	18 300	3 800	5 000	0,90	33210	3DE			
	100	36	154 000	200 000	22 800	3 800	5 000	1,30	T2ED 050	2ED			
	105	32	108 000	137 000	16 000	3 200	4 300	1,20	T7FC 050	7FC			

Needle roller bearings with flanges
with inner ring
d 40–65 mm



Series NA 69

Series NK(S), NA 49

Principal dimensions		Basic load ratings		Fatigue load limit		Speed ratings		Mass		Designation	
d	D	B	C	C ₀	P _u	grease	oil				
mm		N		N		r/min		kg			
40	55	20	27 500	57 000	7 200	6 300	9 000	0.14		NK1 40/20	
	55	30	40 200	93 000	12 000	6 300	9 000	0.22		NK1 40/30	
	62	22	42 900	91 500	8 000	5 600	8 000	0.23		NA 4908	
	62	40	67 100	125 000	16 000	5 600	8 000	0.43		NA 4908	
	65	22	42 900	72 000	9 150	5 600	8 000	0.28		NK1S 40	
42	57	20	29 200	61 000	7 650	6 000	8 500	0.15		NK1 42/20	
	57	30	41 800	98 000	12 900	6 000	8 500	0.22		NK1 42/30	
45	62	25	38 000	78 000	10 000	5 600	8 000	0.23		NK1 45/25	
	62	35	49 500	110 000	14 300	5 600	8 000	0.32		NK1 45/35	
	68	22	45 700	78 000	10 000	5 300	7 500	0.27		NA 4909	
	68	40	70 400	137 000	17 300	5 300	7 500	0.50		NA 4909	
	72	22	44 600	78 000	10 000	5 000	7 000	0.34		NK1S 45	
50	68	25	40 200	88 000	11 200	5 300	7 500	0.27		NK1 50/25	
	68	35	52 300	122 000	16 000	5 300	7 500	0.38		NK1 50/35	
	72	22	47 300	85 000	11 000	5 000	7 000	0.27		NA 4910	
	72	40	73 700	150 000	19 000	5 000	7 000	0.52		NA 4910	
	80	28	62 700	104 000	13 700	4 500	6 300	0.52		NK1S 50	
55	72	25	41 800	96 500	12 200	4 800	6 700	0.27		NK1 55/25	
	72	35	55 000	134 000	17 600	4 800	6 700	0.38		NK1 55/35	
	80	25	57 200	105 000	13 700	4 500	6 300	0.40		NA 4911	
	80	45	89 700	180 000	24 000	4 500	6 300	0.78		NA 4911	
	85	28	66 000	114 000	15 000	4 300	6 000	0.56		NK1S 55	
60	82	25	44 000	95 000	12 000	4 300	6 000	0.40		NK1 60/25	
	82	35	60 500	146 000	19 000	4 300	6 000	0.55		NK1 60/35	
	85	25	60 500	114 000	14 600	4 300	6 000	0.43		NA 4912	
	85	45	93 500	204 000	28 000	4 300	6 000	0.81		NA 4912	
	90	28	68 200	120 000	15 600	4 000	5 600	0.56		NK1S 60	
65	90	25	61 600	120 000	15 300	4 000	5 600	0.46		NA 4913	
	90	35	82 800	168 000	21 600	4 000	5 600	0.47		NK1 65/25	
	90	45	95 200	212 000	27 000	4 000	5 600	0.66		NK1 65/35	
	90	45	95 200	212 000	27 000	4 000	5 600	0.83		NA 4913	
	95	28	70 400	132 000	17 000	3 800	5 300	0.64		NK1S 65	

**Engineering Tripos Part IIA: Module 3C8
Machine Design**

Numerical answers – 2026

1. (a) 1.08 GPa, (b) 43.8 μm , (c) 335 MPa, 2.86 mm, (d) 99.939%
2. (b) 3.08, 1.51, 1408 s. (e) 500 m
- 3 (a) (iii) 223 kN
4. (c) (i) 147 Nm, (ii) 7.32 mm, (iii) 9.42 Nm